
2023 X:AI ADV Session
Toy Project 최종 발표

Formula To Latex

CV2 Team
황건하 이승학 유광열 이서연

Team Member



황건하
행정학전공 16

이승학
시빅데이터융합경영 18



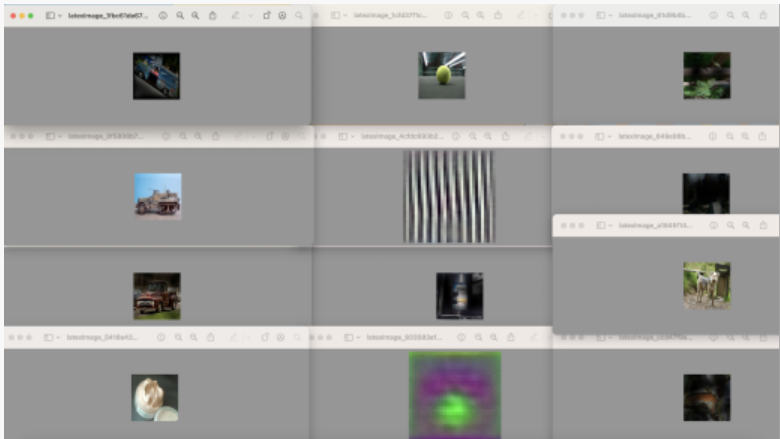
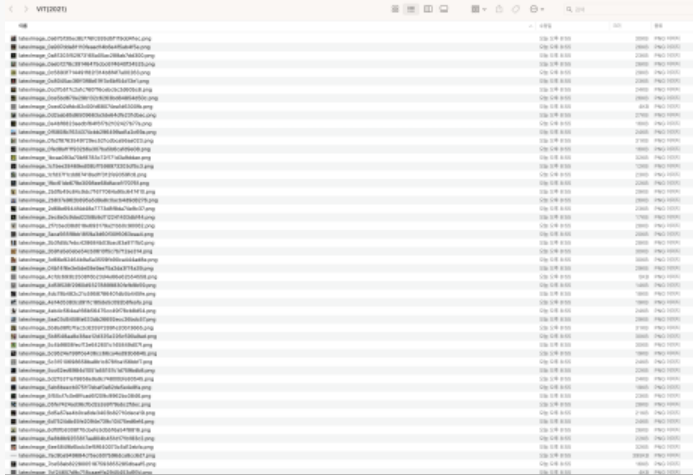
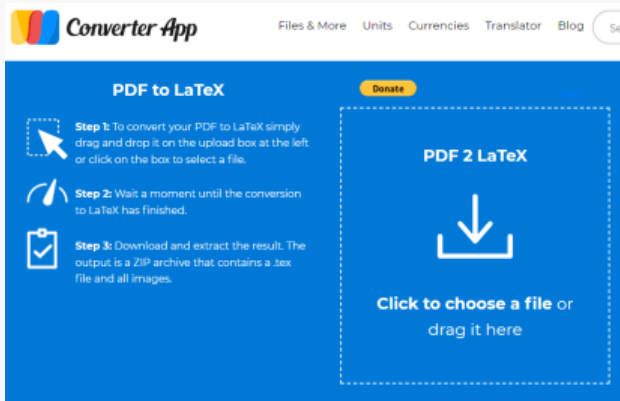
유광열
시빅데이터융합경영 19

이서연
시빅데이터융합경영 21

연구 배경

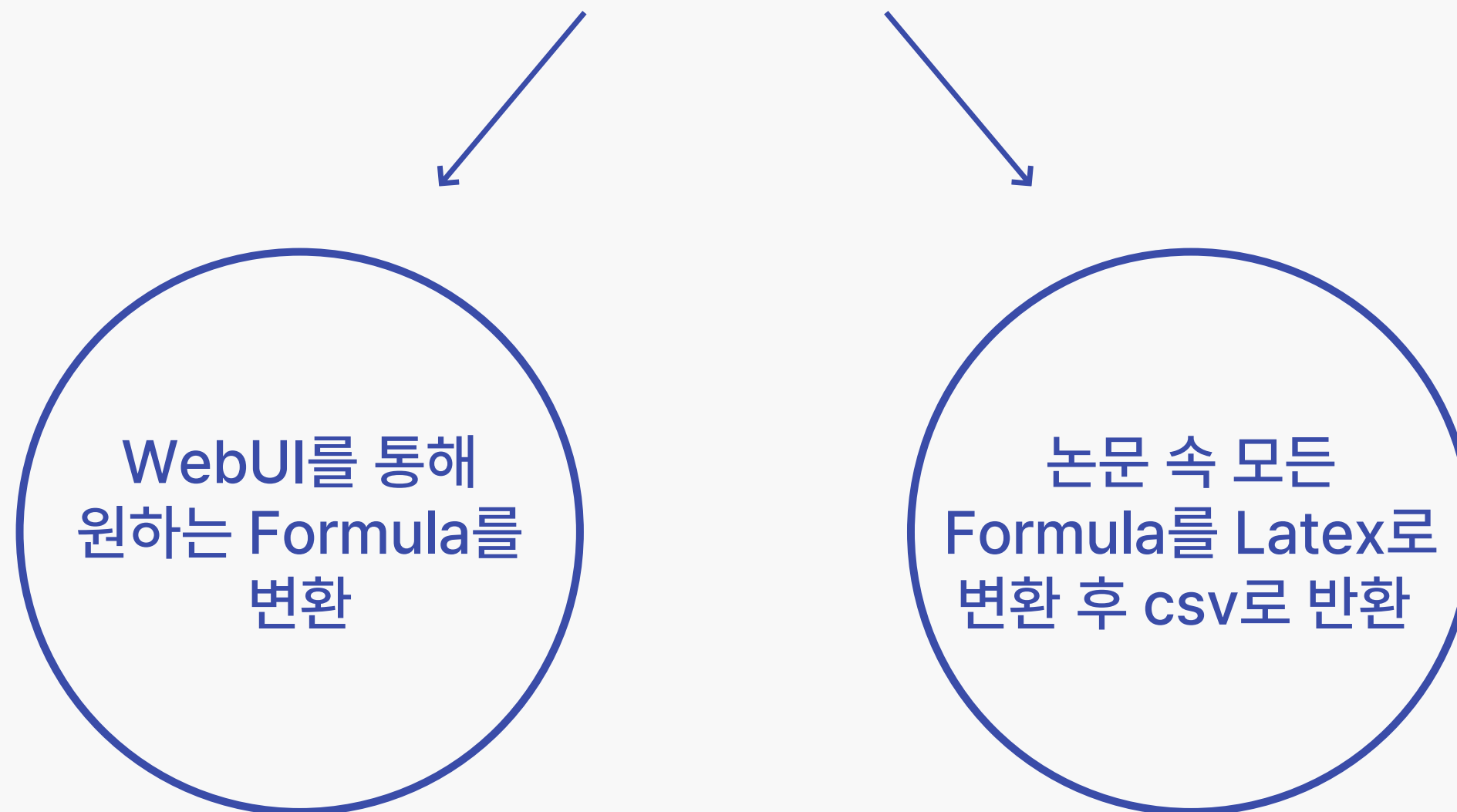
1. 논문 번역 시 수식 변환의 어려움 존재

2. 기존에 존재하는 PDF to LaTeX가 제대로 작동되지 않음



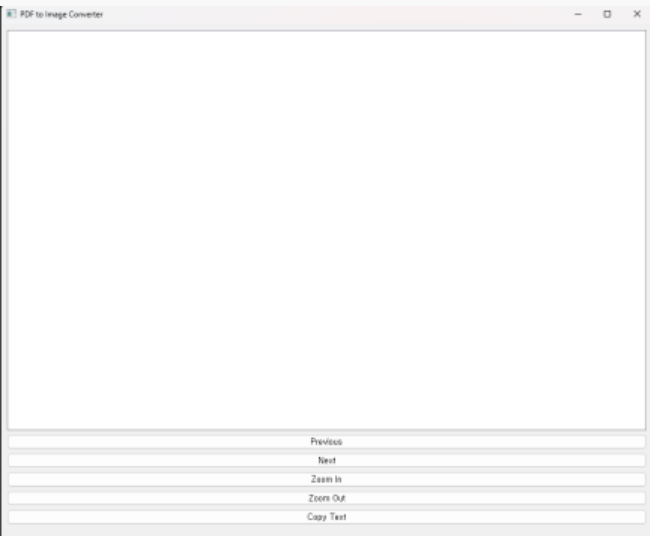
주제

Formula To Latex

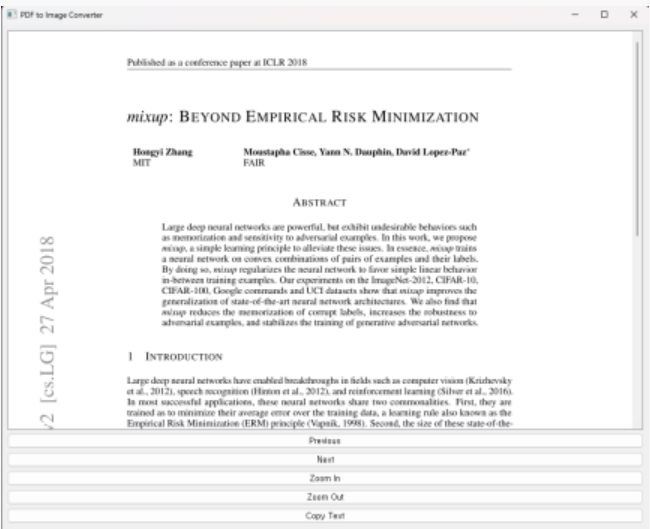


Method1 - WebUI를 통해 원하는 Formula를 변환

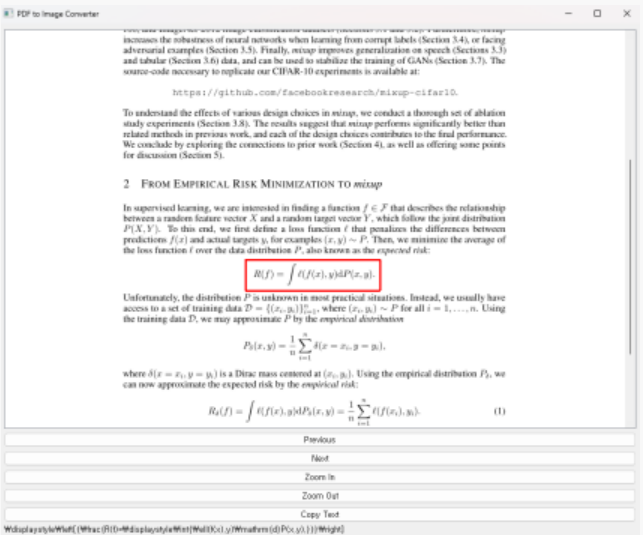
WebUI 실행



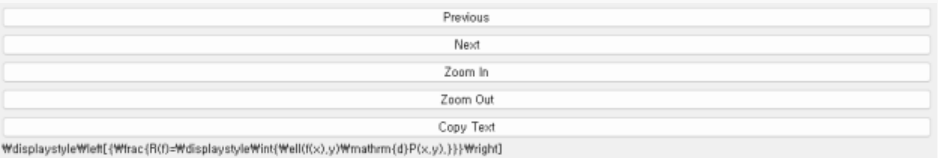
PDF 형식의 논문 드래그



원하는 Formula 영역 지정



변환된 Latex 언어 복사하여 사용

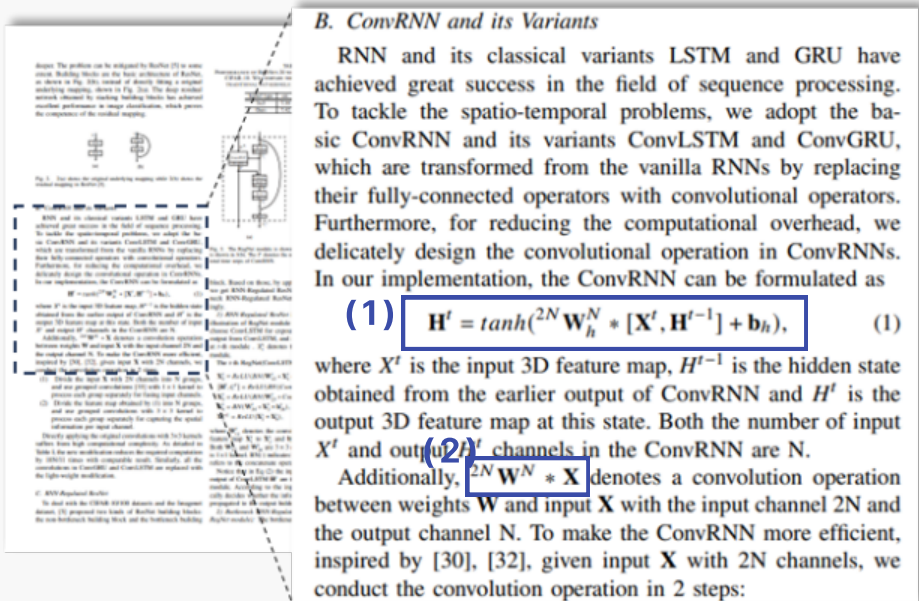


Method2 - 논문 속 모든 Formula를 Latex로 변환 후 csv로 반환

Input



Formula Detection



(1)

$$\mathbf{H}^t = \tanh({}^{2N}\mathbf{W}_h^N * [\mathbf{X}^t, \mathbf{H}^{t-1}] + \mathbf{b}_h),$$

(2)

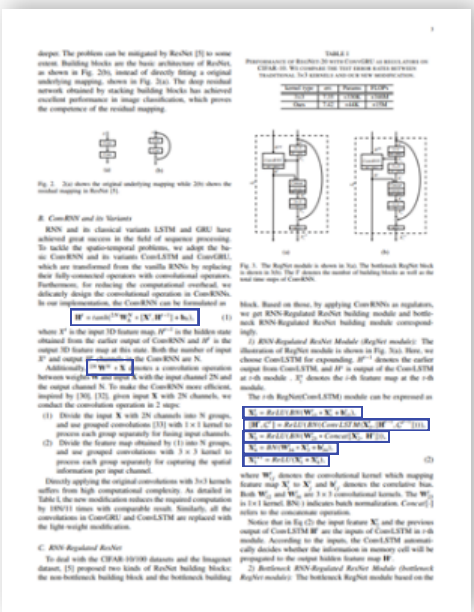
$${}^{2N}\mathbf{W}^N * \mathbf{X}$$

Image To Latex

$$\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{H}\}^{\wedge}\{\mathbf{t}\}=\mathbf{t}\mathbf{a}\mathbf{n}\mathbf{h}(\{\}^{\wedge}\{2\mathbf{N}\}\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{W}\}_{\mathbf{h}}^{\wedge}\{\mathbf{N}\}\mathbf{W}\mathbf{a}\mathbf{s}\mathbf{t}[\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{X}\}^{\wedge}\{\mathbf{t}\},\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{H}\}^{\wedge}\{\mathbf{t}-1\}]+\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{b}\}_{\mathbf{h}}\},$$

$$^{\wedge}\{2\mathbf{N}\}\mathbf{W}^{\wedge}\{\mathbf{N}\} * \mathbf{X}$$

Output



No	Latex
1	$\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{H}\}^{\wedge}\{\mathbf{t}\}=\mathbf{t}\mathbf{a}\mathbf{n}\mathbf{h}(\{\}^{\wedge}\{2\mathbf{N}\}\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{W}\}_{\mathbf{h}}^{\wedge}\{\mathbf{N}\}\mathbf{W}\mathbf{a}\mathbf{s}\mathbf{t}[\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{X}\}^{\wedge}\{\mathbf{t}\},\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{H}\}^{\wedge}\{\mathbf{t}-1\}]+\{\mathbf{W}\mathbf{b}\mathbf{f}\mathbf{b}\}_{\mathbf{h}}\},$
2	$^{\wedge}\{2\mathbf{N}\}\mathbf{W}^{\wedge}\{\mathbf{N}\} * \mathbf{X}$

Task1 - Formula Detection

문서, 이미지 or 스캔된 페이지에서 수학 공식 or 수학적 표현을 자동으로 위치

which after substitution in Eq. (12) leads to

$$\alpha^2 - D\beta^2 = \frac{d_k^2 N^2 R_0^4}{4}.$$
 (14)

In these coordinates the dilaton, or equivalently the string coupling squared, is $e^{2\phi} = e^{2\sigma} = M^{-1} \eta^D R^{d_k}$ and the Kalb-Ramond field strength is $H = N R^4 dt \wedge \mathcal{J}$.

Although there is a world of possibilities in the above class of solutions, perhaps the most interesting case is the one where $\beta_k = 0$, since then the uncompactified part of spacetime is just Minkowski space: Taking $\sigma = 0$ for convenience, one finds that the solution in, string, cosmological time, τ , reads

$$\begin{aligned} ds^2 &= d\tau^2 - d\vec{x}_{(D)}^2 - 2h_0^2 B(\tau)^{-1} h_{mn} dy^m dy^n, \\ e^{2\phi} &= \left(\sqrt{2}R_0\right)^{d_k} \tau^{-1} B(\tau)^{-d_k/2}, \\ H &= 8R_0^2 d_k^{-1/2} \tau^{-1} B(\tau)^{-2} d\tau \wedge \mathcal{J}, \\ B(\tau) &= \tau^{2/\sqrt{d_k}} + \tau^{-2/\sqrt{d_k}}. \end{aligned}$$
 (15)

As one can see, this is a completely regular solution, modulo the usual gravitational singularities, which smoothly interpolates between two Kasner-like regions [6]. From the lower dimensional point of view, the Ansatz considered above corresponds to a solution of dilaton-gravity coupled to moduli [10], where the breathing mode, B , and \mathcal{J} are the scalar fields parameterizing an $SL(2, \mathbb{R})/U(1)$ coset model. When $\beta_k = 0$, the above solutions can be obtained from the solutions given in [2] by applying an $SL(2, \mathbb{R})$ transformation on the moduli.

2 RR case

In much the same way as in the foregoing subsection, we can use the RR two form in type IIA, to trigger compactification. In this case the equations of motion and the Bianchi identity imply that

$$F_{(2)} = N \mathcal{J} = \frac{1}{2} N \mathcal{J}_{mn} dy^m \wedge dy^n.$$
 (17)

Applying the same steps as in the foregoing paragraph, one finds

$$\begin{aligned} 0 &= (\log R)'' + \frac{(d_k-4)N^2}{8} M \eta^D R^{d_k-4}, \\ 0 &= (\log \eta)'' + \frac{d_k N^2}{8} M \eta^D R^{d_k-4} - \lambda \eta^{-2} M^2, \\ 0 &= (\log M)'' - \frac{d_k N^2}{8} M \eta^D R^{d_k-4} - D \lambda \eta^{-2} M^2, \\ 0 &= [(\log M)]'^2 - D [(\log \eta)]'^2 - d_k [(\log R)]'^2 - \frac{d_k N^2}{8} M \eta^D R^{d_k-4} - D \lambda M^2 \eta^{-2}. \end{aligned}$$
 (18)

Looking at the above expressions, one sees that they simplify enormously when one considers the case $\beta_k = 0$. In that case the Kähler breathing mode decouples completely and one has $R = R_0 e^{\sigma}$. Equating also the powers of N and η in the equations, i.e. putting $M = d_k^{-D/2}$, one necessarily has to impose

$$\lambda = \frac{N^2}{4} (D+3).$$
 (22)

which after substitution in Eq. (12) leads to

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$$\lambda = \frac{N^2}{4} (D+3).$$
 (22)

1. 텍스트 감지

→ 문서의 텍스트 영역을 감지

2. 공식 구별

→ 감지된 텍스트 영역 중에서 수학 공식 or 수식을 포함하고 있는 영역을 구별

3. 공식 위치 파악

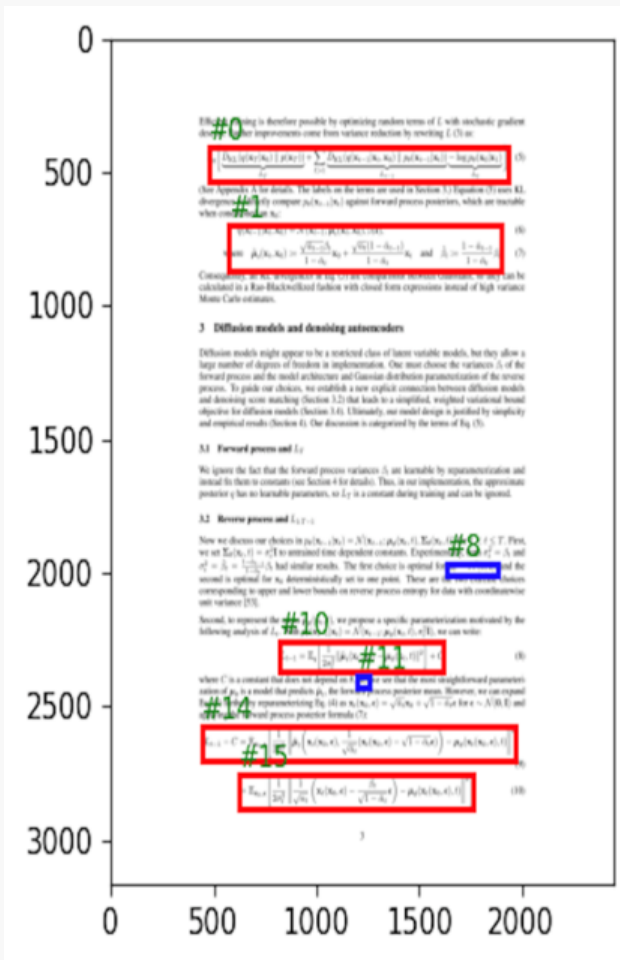
→ 수학 공식의 정확한 위치와 경계 파악

Task1 - Formula Detection

Model

CnSTD (Chinese Scene Text Detector)

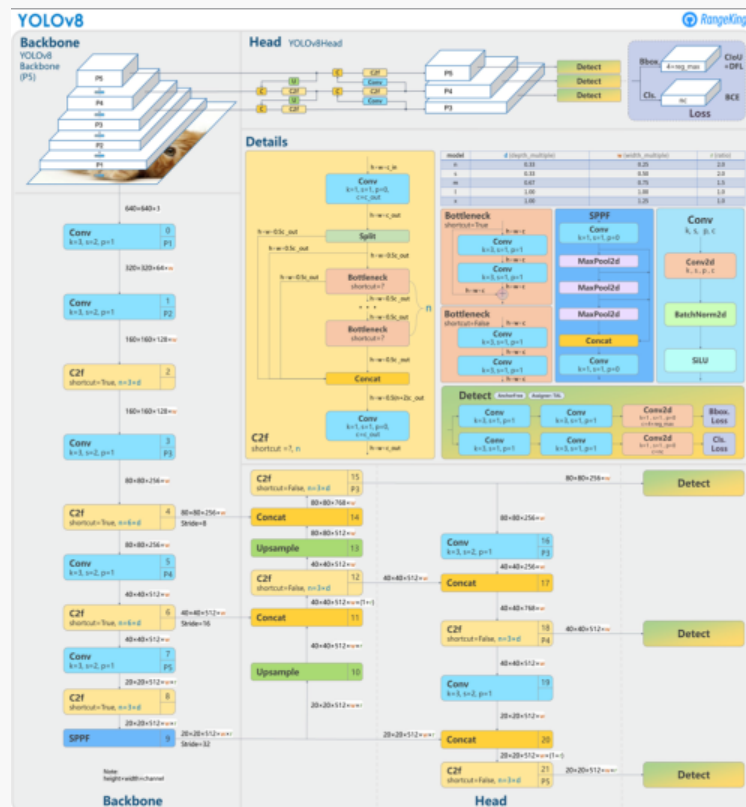
Inference



Task1 - Formula Detection

Model

YOLO v8



YOLO 모델을 위한 완전히 새로운 리포지토리를 출시하여
개체 감지, 인스턴스 세분화 및 이미지 분류 모델을 train하기
위한 통합 프레임워크로 구축

- YOLOv8n, YOLOv8x, YOLOv8m 등 다양한 버전이 존재
- YOLOv8m (medium)은 COCO에서 50.2의 mAP 달성

Inference

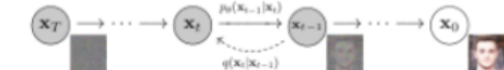


Figure 2: The directed graphical model considered in this work.

This paper presents progress in diffusion probabilistic models [53]. A diffusion probabilistic model (which we will call a “diffusion model” for brevity) is a parameterized Markov chain trained using variational inference to produce samples matching the data after finite time. Transitions of this chain are learned to reverse a diffusion process, which is a Markov chain that gradually adds noise to the data in the opposite direction of sampling until signal is destroyed. When the diffusion consists of small amounts of Gaussian noise, it is sufficient to set the sampling chain transitions to conditional Gaussians too, allowing for a particularly simple neural network parameterization.

Diffusion models are straightforward to define and efficient to train, but to the best of our knowledge, there has been no demonstration that they are capable of generating high quality samples. We show that diffusion models actually are capable of generating high quality samples, sometimes better than the published results on other types of generative models (Section 4). In addition, we show that a certain parameterization of diffusion models reveals an equivalence with denoising score matching over multiple noise levels during training and with annealed Langevin dynamics during sampling (Section 3.2) [55, 61]. We obtained our best sample quality results using this parameterization (Section 4.2), so we consider this equivalence to be one of our primary contributions.

Despite their sample quality, our models do not have competitive log likelihoods compared to other likelihood-based models (our models do, however, have log likelihoods better than the large estimates annealed importance sampling has been reported to produce for energy based models and score matching [11, 55]). We find that the majority of our models’ lossless code lengths are consumed to describe imperceptible image details (Section 4.3). We present a more refined analysis of this phenomenon in the language of lossy compression, and we show that the sampling procedure of diffusion models is a type of progressive decoding that resembles autoregressive decoding along a bit ordering that vastly generalizes what is normally possible with autoregressive models.

2 Background

Diffusion models [53] are latent variable models of the form $p_\theta(\mathbf{x}_0) := \int p_\theta(\mathbf{x}_{0:T}) d\mathbf{x}_{1:T}$, where $\mathbf{x}_1, \dots, \mathbf{x}_T$ are latents of the same dimensionality as the data $\mathbf{x}_0 \sim q(\mathbf{x}_0)$. The joint distribution $p_\theta(\mathbf{x}_{0:T})$ is called the *reverse process*, and it is defined as a Markov chain with learned Gaussian transitions starting at $p(\mathbf{x}_T) = \mathcal{N}(\mathbf{x}_T; \mathbf{0}, \mathbf{I})$.

$$p_\theta(\mathbf{x}_{0:T}) = p(\mathbf{x}_T) \prod_{t=1}^T p_\theta(\mathbf{x}_{t-1} | \mathbf{x}_t), \quad p_\theta(\mathbf{x}_{t-1} | \mathbf{x}_t) = \mathcal{N}(\mathbf{x}_{t-1}; \mu_\theta(\mathbf{x}_t, t), \Sigma_\theta(\mathbf{x}_t, t)) \quad (1)$$

What distinguishes diffusion models from other types of latent variable models is that the approximate posterior $q(\mathbf{x}_{1:T} | \mathbf{x}_0)$ called the *forward process* or *diffusion process*, is fixed to a Markov chain that gradually adds Gaussian noise to the data according to a variance schedule β_1, \dots, β_T :

$$q(\mathbf{x}_{1:T} | \mathbf{x}_0) = \prod_{t=1}^T q(\mathbf{x}_t | \mathbf{x}_{t-1}), \quad q(\mathbf{x}_t | \mathbf{x}_{t-1}) = \mathcal{N}(\mathbf{x}_t; \sqrt{1 - \beta_t} \mathbf{x}_{t-1}, \beta_t \mathbf{I}) \quad (2)$$

Training is performed by optimizing the neural variational bound on negative log likelihood:

$$\mathbb{E}[-\log p_\theta(\mathbf{x}_0)] \leq \mathbb{E}\left[-\log \frac{p_\theta(\mathbf{x}_{0:T})}{q(\mathbf{x}_{1:T} | \mathbf{x}_0)}\right] = \mathbb{E}_q\left[-\log p(\mathbf{x}_T) - \sum_{t=1}^T \log \frac{p_\theta(\mathbf{x}_{t-1} | \mathbf{x}_t)}{q(\mathbf{x}_t | \mathbf{x}_{t-1})}\right] = L \quad (3)$$

The forward process variances β_t can be learned by reparameterization [33] or held constant as hyperparameters, and expressiveness of the reverse process is ensured in part by the choice of Gaussian conditionals in $p_\theta(\mathbf{x}_{t-1} | \mathbf{x}_t)$, because both processes have the same functional form when β_t are small [53]. A notable property of the forward process is that it admits sampling \mathbf{x}_t at an arbitrary timestep t in closed form: using the notation $\alpha_t := 1 - \beta_t$ and $\bar{\alpha}_t := \prod_{s=1}^t \alpha_s$ we have

$$q(\mathbf{x}_t | \mathbf{x}_0) = \mathcal{N}(\mathbf{x}_t; \sqrt{\bar{\alpha}_t} \mathbf{x}_0, (1 - \bar{\alpha}_t) \mathbf{I}) \quad (4)$$

Task1 - Formula Detection

Data 생성

Grad-CAM: Visual Explanations from Deep Networks via Gradient-based Localization 5

to successive matrix products of the weight matrices and the gradient with respect to activation functions till the final convolution layer that the gradients are being propagated to. Hence, this weight α_k^c represents a *partial linearization* of the deep network downstream from A , and captures the 'importance' of feature map k for a target class c .

We perform a weighted combination of forward activation maps, and follow it by a ReLU to obtain,

$$L_{\text{Grad-CAM}}^c = \text{ReLU} \left(\underbrace{\sum_k \alpha_k^c A^k}_{\text{linear combination}} \right) \quad (2)$$

Notice that this results in a coarse heatmap of the same size as the convolutional feature maps (14×14 in the case of last convolutional layers of VGG [52] and AlexNet [33] networks)³. We apply a ReLU to the linear combination of maps because we are only interested in the features that have a *positive* influence on the class of interest, *i.e.* pixels whose intensity should be *increased* in order to increase y^c . Negative pixels are likely to belong to other categories in the image. As expected, without this ReLU, localization maps sometimes highlight more than just the desired class and perform worse at localization. Figures 1c, 1f and 1i, 1l show Grad-CAM visualizations for 'tiger cat' and 'boxer (dog)' respectively. Ablation studies are available in Sec. B.

In general, y^c need not be the class score produced by an image classification CNN. It could be any differentiable activation including words from a caption or answer to a question.

3.1 Grad-CAM generalizes CAM

In this section, we discuss the connections between Grad-CAM and Class Activation Mapping (CAM) [59], and formally prove that Grad-CAM generalizes CAM for a wide variety of CNN-based architectures. Recall that CAM produces a localization map for an image classification CNN with a specific kind of architecture where global average pooled convolutional feature maps are fed directly into softmax. Specifically, let the penultimate layer produce K feature maps, $A^k \in \mathbb{R}^{u \times v}$, with each element indexed by i, j . So A_{ij}^k refers to the activation at location (i, j) of the feature map A^k . These feature maps are then spatially pooled using Global Average Pooling (GAP) and linearly transformed to produce a score Y^c for each class c ,

$$Y^c = \sum_k \underbrace{w_k^c}_{\text{class feature weights}} \underbrace{\frac{1}{Z} \sum_i \sum_j A_{ij}^k}_{\text{feature map}} \quad (3)$$

³ We find that Grad-CAM maps become progressively worse as we move to earlier convolutional layers as they have smaller receptive fields and only focus on less semantic local features.

Let us define F^k to be the global average pooled output,

$$F^k = \frac{1}{Z} \sum_i \sum_j A_{ij}^k \quad (4)$$

CAM computes the final scores by,

$$Y^c = \sum_k w_k^c \cdot F^k \quad (5)$$

where w_k^c is the weight connecting the k^{th} feature map with the c^{th} class. Taking the gradient of the score for class c (Y^c) with respect to the feature map F^k we get,

$$\frac{\partial Y^c}{\partial F^k} = \frac{\partial Y^c}{\partial A_{ij}^k} \quad (6)$$

Taking partial derivative of (4) w.r.t. A_{ij}^k , we can see that $\frac{\partial F^k}{\partial A_{ij}^k} = \frac{1}{Z}$. Substituting this in (6), we get,

$$\frac{\partial Y^c}{\partial F^k} = \frac{\partial Y^c}{\partial A_{ij}^k} \cdot Z \quad (7)$$

From (5) we get that, $\frac{\partial Y^c}{\partial F^k} = w_k^c$. Hence,

$$w_k^c = Z \cdot \frac{\partial Y^c}{\partial A_{ij}^k} \quad (8)$$

Summing both sides of (8) over all pixels (i, j) ,

$$\sum_i \sum_j w_k^c = \sum_i \sum_j Z \cdot \frac{\partial Y^c}{\partial A_{ij}^k} \quad (9)$$

Since Z and w_k^c do not depend on (i, j) , rewriting this as

$$Z w_k^c = Z \sum_i \sum_j \frac{\partial Y^c}{\partial A_{ij}^k} \quad (10)$$

Note that Z is the number of pixels in the feature map (or $Z = \sum_i \sum_j 1$). Thus, we can re-order terms and see that

$$w_k^c = \sum_i \sum_j \frac{\partial Y^c}{\partial A_{ij}^k} \quad (11)$$

Up to a proportionality constant ($1/Z$) that gets normalized out during visualization, the expression for w_k^c is identical to α_k^c used by Grad-CAM (1). Thus, Grad-CAM is a strict generalization of CAM. This generalization allows us to generate visual explanations from CNN-based models that cascade convolutional layers with much more complex interactions, such as those for image captioning and VQA (Sec. 8.2).

8개의 논문 이용



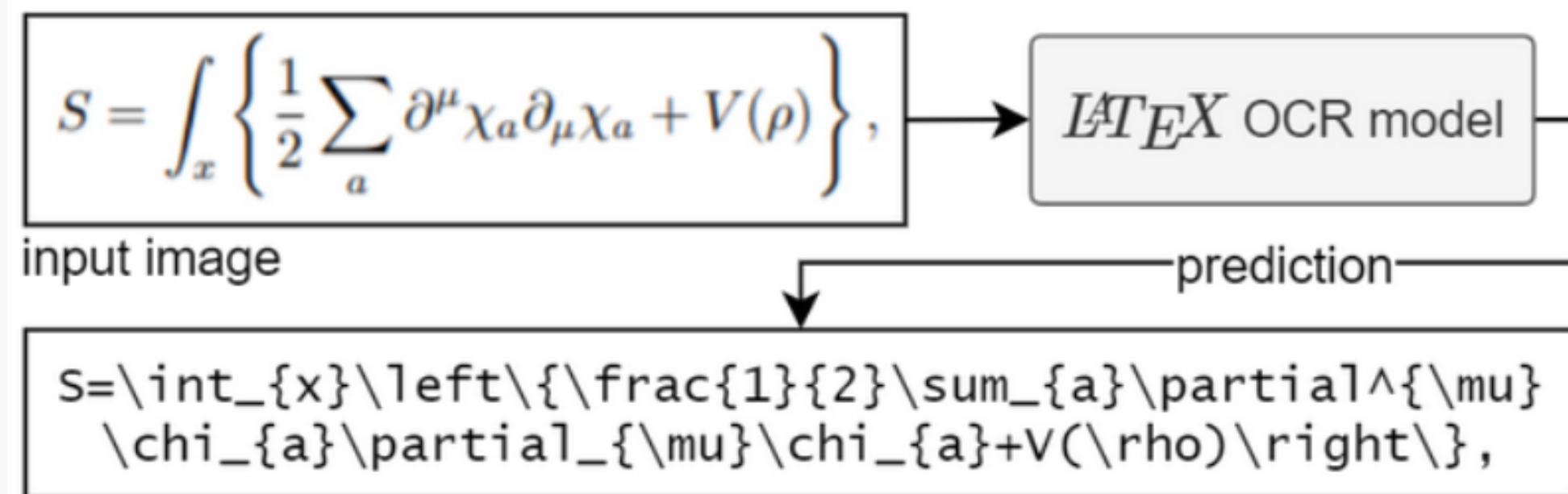
Labeling

1	0.752648	0.310044	0.125567	0.062227
2	0.826778	0.362991	0.031770	0.022926
3	0.554841	0.387009	0.080938	0.031659
4	0.747731	0.430131	0.158094	0.048035
5	0.725794	0.480349	0.088502	0.027293
6	0.746218	0.526474	0.135401	0.040939
7	0.746974	0.617631	0.276097	0.049672
8	0.627080	0.667303	0.033283	0.019105
9	0.745461	0.713155	0.203480	0.045306
10	0.584720	0.777838	0.065053	0.025109
11	0.740545	0.827511	0.178517	0.051310
12	0.791982	0.871998	0.052950	0.019105
13	0.858926	0.892194	0.029501	0.019105
14	0.526475	0.909389	0.036309	0.019651

→ 학습까지 완료

Task2 - Formula To Latex

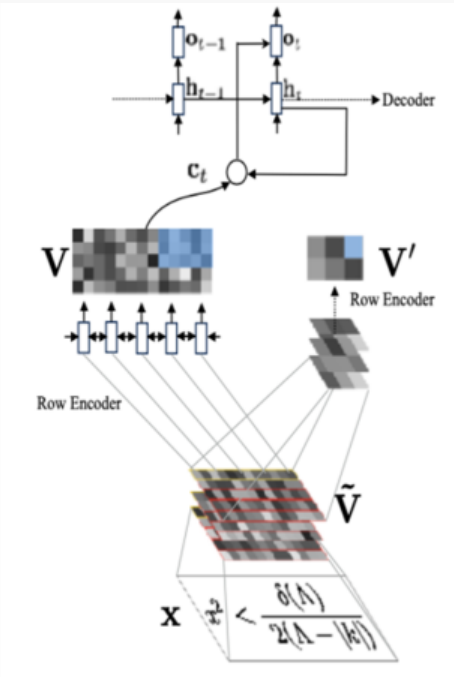
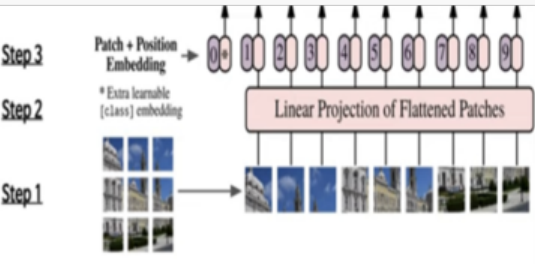
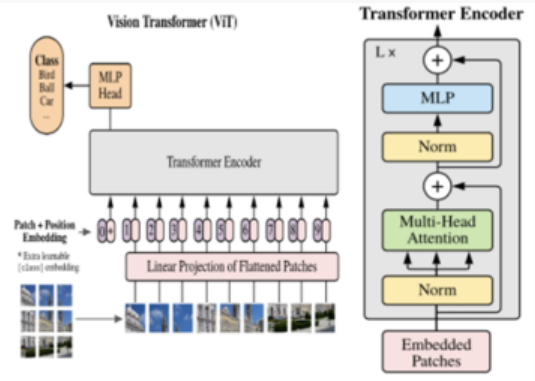
수학 공식을 LaTeX 형식으로 변환하는 도구나 알고리즘



Task2 - Formula To Latex

Model

pix2tex - LatexOCR



$$\Psi = \exp (i l \varphi) R(\rho) .$$

$$\xi_n(u)=\sin\Big(\frac{\pi n u}{t}\Big) \qquad n=1,2,\ldots$$

$$\delta^V(t)g=g((t^2-1)\dot{X}(t)X(t)^{-1}+I),$$

$$\partial_z^2 H_F + H_p \partial_x^2 H_F = 0, \quad \partial_z^2 H_p = 0.$$

Inference



Task2 - Formula To Latex

Data

M2LATEX-100K (Kaggle)

```
{ \cal L } _ { a
) _ { i j } = 0 ,
\ \ ( { \cal L
{ a } H ) _ { i j
} = 0 ,
```

```
S _ { s t a t } =
\pi \sqrt { N _ {
} ^ { ( 1 ) } } N _
5 } ^ { ( 2 ) } N
{ 5 } ^ { ( 3 ) }
...
```

```
\frac { \phi ^
prime \prime } {
} } + { \frac {
{ A } } } \left(
\frac { 1 } { 2 }

```

```
+ \int \! \! \! d ^ {
} \! \! z _ { 1 } d ^
D } \! \! z _ { 2 } d
{ D } \! \! z _ { 3 }
\left. \frac {
\mathrm{d} \dots

```

WebUI Inference

Formula Extract Inference

기대효과

논문 리뷰 작성할 때
수식 입력이 편해짐

처음보는 수학 기호에
대한 Latex를
찾아볼 필요가 없음

전체 논문 번역 시
자연스러운 번역 결과가
나올 것으로 기대

결론

아쉬운 점

- WebUI에서 드래그 하는 영역의 빨간 박스가 Latex모델에 같이 전달되는 문제
- WebUI를 예쁘게 만들지 못함
- 대량의 데이터를 활용하지 못함

$$(x, y, z, \theta, \phi)$$

앞으로의 계획

- 학습된 YOLO 모델 적용
- TTS -> Latex 언어로 변환된 Formula를 Speech로 읽는 법을 알려줌
- Formula를 Latex로 변환하여 논문 전체를 한번에 Translation
- 배포